

Objective: To read & write **integers**
To **graph** integers on a **number line**

Date: _____

Introduction to Integers

The Examples:

What does an integer look like?

{...-3, -2, -1, 0, 1, 2, 3...}

↑
Zero is not positive or negative.

Write an Integer for each Situation:

1) *falling 6 feet*

A: **-6 ft**

2) *a profit of \$12*

A: **+\$12 or \$12**

3) *22° F below 0*

A: **-22° F**

Explanation:

An **integer** is any **positive** or **negative** whole number

Which integers are less than zero?

- **Negative Integers**

Which integers greater than zero?

- **Positive Integers**

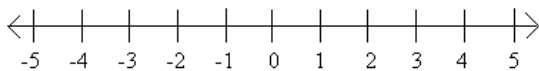
Don't forget **labels!!

Fact: The **+** sign is optional. If you do not see the **+** sign in front of a number, it is understood to be **positive**.

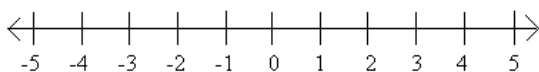
Graphing Integers

The Examples:

4) Graph the set of integers $\{-1, 3, -2\}$

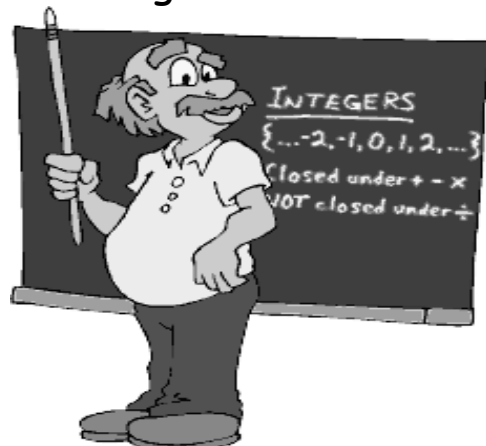


5) Graph the set of integers $\{-2, 1, -4, 0\}$



Explanation:

To graph an integer, you will need a **number line**. Draw a **point** at the location of each integer.



Objective: To find the **absolute value** of a number
To **evaluate** expressions

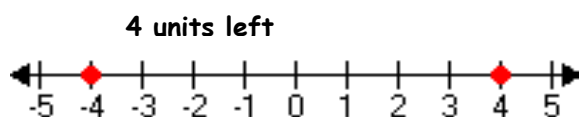
Date: _____

Absolute Value

The Examples:

1) Evaluate the expression $|-4|$

On the number line, the graph of -4 is 4 units from 0.



So, $|-4| = 4$

2) $|11| = 11$

Explanation:

Absolute value of a number is its **distance** from **zero** on the number line.

Two vertical **bars** are used to represent absolute value.

The symbol for the absolute value of -4 is $|-4|$

The numbers 4 and -4 are the same **distance** from 0. So, 4 and -4 have the same **absolute value**

3) Evaluate the Expression:

$$|-4| - |3| = 4 - 3 \\ = 1$$

4) $9 + |-6| \div 1^2$

$$9 + 6 \div 1^2$$

$$9 + 6 \div 1$$

$$9 + 6$$

$$15$$

Remember $|-4| = 4$, $|3| = 3$
Subtract.

*Rewrite the problem without absolute value

*Follow PEMDAS!!! First do **exponents**

*Then **divide**

*Finally **add**

Objective: To **compare** Integers

Date: _____

Comparing Integers

The Examples:

Replace each ○ with < or > to make a true sentence.

1. \$5 < \$8

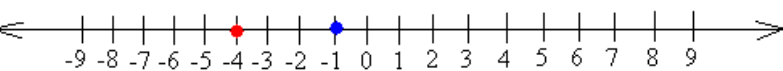
2. -\$2 < \$10

3. \$3 = +\$3

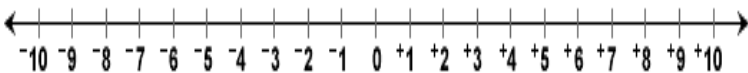


Trick Question!!!

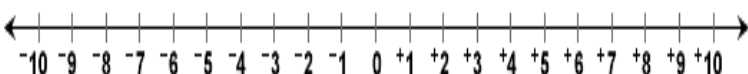
1. -1 > -4



2. -2 > -5



3. | -4 | > 3



Explanation:

This symbol < means **less than**.

This symbol > means **greater than**.

The alligator eats the **bigger** number!



****Don't forget that the + sign is optional. If you do not see the + sign in front of a number, it is understood to be positive.**

When two numbers are graphed on a number line, the number to the left is always **less than** the number to the **right**. Thus, the number to the right is always **greater than** the number to the left.

Hint: It helps to first graph the numbers!

****Don't forget that absolute value is always positive. So, | -4 | = 4**

Ordering Integers

The Examples:

Order the integers from least to greatest:

4. 12, -6, 20, -47, -11

A: **-47, -11, -6, 12, 20**

5. $|-13|$, 0, 7, -8, -5, $|2|$

A: **-8, -5, 0, 2, 7, 13**

Explanation:

Remember: Order integers on the number line from **left** to **right** for least to greatest.

Remember: $|-13| = 13$ and $|2| = 2$

Determine whether each sentence is *True* or *False*. If **False**, change ONE number to make the sentence true.

6. $-7 < 3$

A: **True**

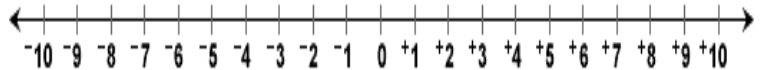
7. $-20 < -22$

A: **False; $-20 < +22$**

8. $3 > |-5|$

A: **False; $3 > |-2|$**

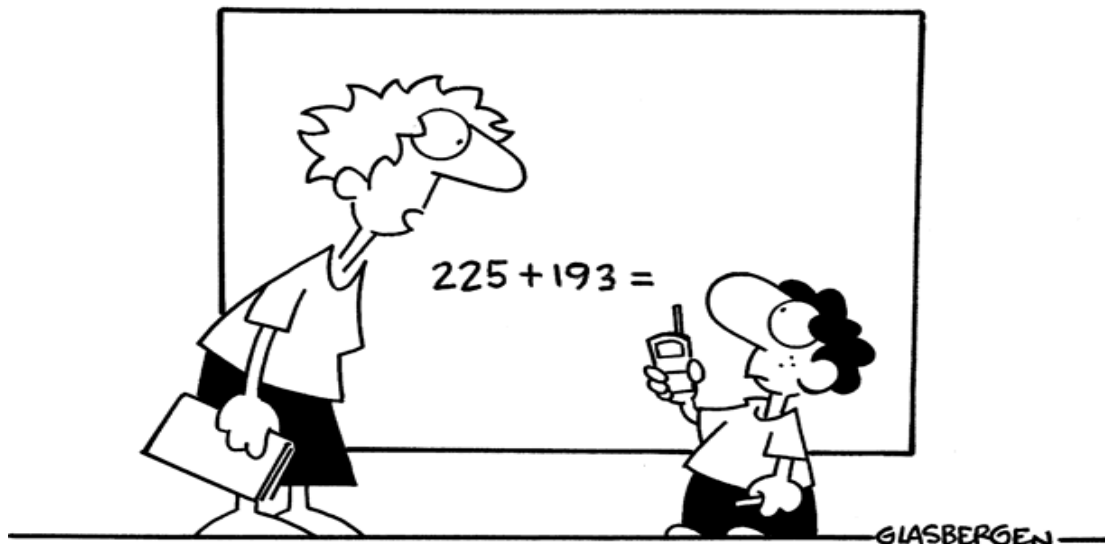
Think: Which is bigger -7 than 3? **3**



Think: The $|-5|$ is **5**

So is 3 or $|-5|$ bigger? **5**

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“You have to solve this problem by yourself. You can’t call tech support.”

Adding Integers

The Examples:

- 1) $5 + 3 = 8$
- 2) $-5 + -3 = -8$
- 3) $5 + -3 = 2$
- 4) $-5 + 3 = -2$

Explanation:

What pattern do you notice?

*Same signs, add the numbers
and keep the sign of the number

*Different signs, subtract the numbers
and take the sign of the farther number

♪ Sounds like a song to me! ♪

(Verse 1)

Same Sign Add and Keep

Different Sign Subtract

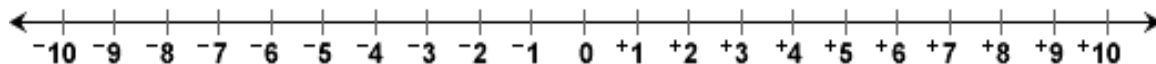
Take the sign of the farther number

Then It'll be Exact

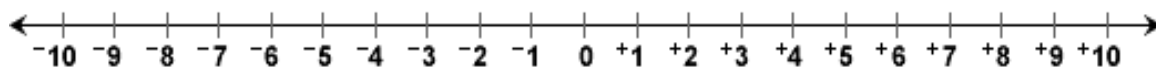
Let's try some more:

Hint: Use a number line to help in the beginning!

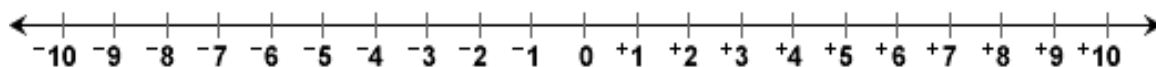
5) $2 + 3 = 5$



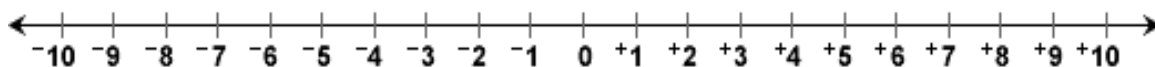
6) $-3 + (-8) = -11$



7) $-7 + 13 = 4$



$6 + (-7) = -1$



Subtracting Integers

As easy as adding integers!

♪ Sing the song and you will know too!! ♪
(Verse 2)

Change the Minus to a Plus
Change the Sign of Next
Then All You Do is Add them Up
As if it were a Plus!

Let's try some examples:

1) $5 - 2 = 3$

2) $-3 - 2 = -5$

3) $15 - (-7) = 22$

4) $-18 - (-40) = 22$

Explanation:

Hint: Use a chart!!

Same	Change	Change
5	+	-2

Same	Change	Change
-3	+	-2

Same	Change	Change
15	+	7

Same	Change	Change
-18	+	40

Evaluate each expression if $r = -4$, $s = 10$, and $t = -7$

5) $r - 7 = -11$

6) $t - s = -17$

	Same	Change	Change
5)	-4	+	-7
6)	-7	+	-10

Objective: To add & subtract Chains of Integers

Date: _____

Chains of Integers



The Examples:

Compute:

$$12 + (+5) + 5 + (-17) + -6 + 5$$

$$--23 + 27$$

The sum of the negatives

The sum of the positives

$$4$$

Final Answer

Explanation:

1. Remember, we like to **ADD!**

So, what do we do with the subtraction signs? (Hint: Think of the song)

Change the minus to a plus

Change the sign of next

2. Now that there are "+" signs between ALL numbers, we need to

circle and **add the negatives**

3. **Add the positive** numbers.

4. Add the two sums for a final answer!

Let's try some more 😊

$$-6 + 7 + 6 + (-7) + (+5) + -13$$

$$-26 + 18$$

$$-8$$

$$5 + (+17) + -5 + (-17) + 8 + 9$$

$$-22 + 39$$

$$17$$



Adding Rules

Same sign add and keep

Different sign subtract

Take the sign of the farther number

Then It'll be exact!

Subtracting Rules

Change the minus to a plus

Change the sign of next

Then all you do is add them up

As if it were a plus! (Ole)

Objective: To multiply Integers

Date: _____

Multiplying Integers

The Examples:

$$2 \times 5 = 10$$

$$-2 \times -5 = 10$$

$$2 \times -5 = -10$$

$$-2 \times 5 = -10$$

$$-2 \times 5 \times -1 = 10$$

$$-2 \times -5 \times -1 = -10$$

Explanation:

REMEMBER: There are three different ways to represent multiplication of two numbers. 2×3 ; $2 \cdot 3$; $2(3)$

Rule:

Count the **negatives**.

* Even number of negatives = + answer

* Odd number of negatives = - answer

Multiply:

1. $-4(6) = -24$

2. $-2(-8) = 16$

3. $-2(-5)(-3) = -30$

4. $-(5)^2 = -(5 \times 5) = -25$

May need to explain how the exponents work with negative numbers.

Evaluate each expression if $g = -5$, $h = -3$, and $k = 4$

5. $7gk$

$$7(-5)(4)$$

$$-35(4)$$

$$-140$$

6. $-2h^2$

$$-2(-3)^2$$

$$-2(9)$$

$$-18$$



Dividing Integers

The Examples:

The rule is the same as multiplying integers. Let's review. \longrightarrow

Explanation:

REMEMBER: There are three different ways to represent division of two numbers. $6 \div 3$, $\frac{6}{3}$, $3 \overline{)6}$

Rule:

Count the **negatives**.

* Even number of negatives = **+** answer

* Odd number of negatives = **-** answer

Divide:

1. $-15 \div 3$ **-5**

2. $-49 \div (-7)$ **7**

3. $\frac{36}{-4}$ **-9**

4. $\frac{0}{-9}$ **0**

Evaluate each expression if $m = -32$, $n = 2$, and $p = -8$

5. $\frac{-p}{n} = \frac{-(-8)}{2} = \frac{8}{2}$ **4**

6. $p \div n^2$
 $-8 \div 2^2$
 $-8 \div 4$
-2

7. $\frac{18-n}{p} = \frac{18-2}{-8} = \frac{16}{-8}$ **-2**



10/3/11 Order of Operations w/ Integers

ex 1: $(4+6) \div 2 + 8 \times 3 - 5$

$10 \div 2 + 8 \times 3 - 5$

$\cancel{5} + 24 \cancel{-5}$
 24

ex 2: $-3 - (5+8)(7+14+11)$

$-3 - -3(-7+11)$

$-3 - -3(4)$

$-3 + +12$

9

ex 3: $[(10)(30) \div 15 \times 4] \div 10 + 10$

$[300 \div 15 \times 4] \div 10 + 10$

$[20 \times 4] \div 10 + 10$

80

$\div 10 + 10$

8 + 10
18

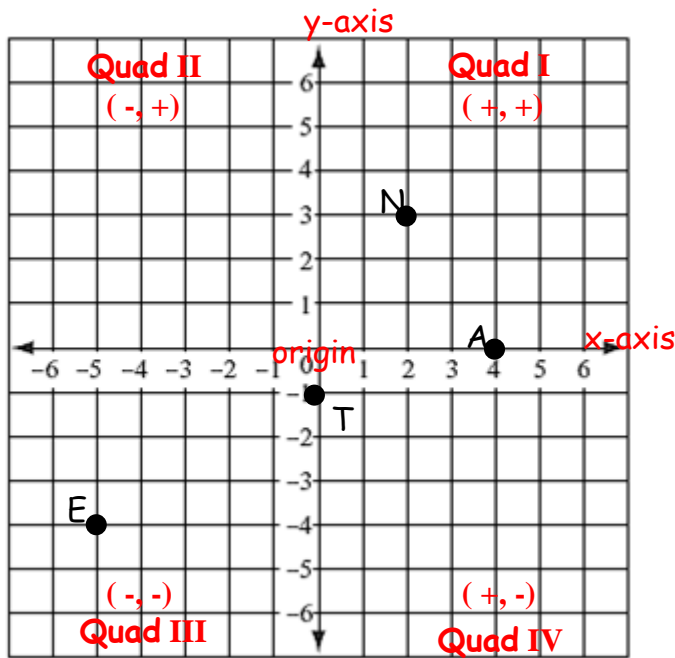
Objective: To graph **points** on a **coordinate plane**. Date: _____

The Coordinate Plane

The Examples:

What does the coordinate plane look like?

The Coordinate Plane



- (____ , ____)
- _____
- _____

answers will vary

Name the ordered pair for the points on the graph above. Then identify the quadrant in which the point lies.

- 1) N (2, 3) Quad I
- 2) E (-5, -4) Quad III
- 3) A (4, 0) x-axis
- 4) T (-1, 0) y-axis

Explanation:

A **coordinate plane** is a plane in which a **horizontal** number line and a vertical number line intersect at their zero points.

- The x-axis is the **horizontal** number line.
- The y-axis is the **vertical** number line.

There are four **quadrants** on a coordinate plane represented by Roman numerals (I, II, III, and IV) that are positioned **counterclockwise** starting at the top right.

An **ordered pair** is a pair of numbers, separated by a comma, used to locate a point on the coordinate plane. The first number is the **x-coordinate**. The second number is the **y-coordinate**. (x, y)

The **origin** is the point at which the x-axis and y-axis intersect in the coordinate plane.

Now, have the students go back to first graph and label the Quads (+, +) etc.

The Coordinate Plane (cont...)

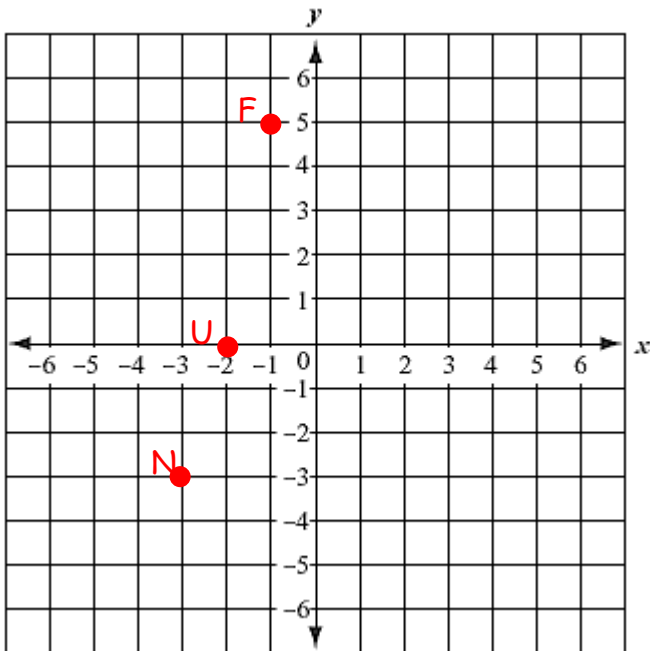
The Examples:

Graph and label each point on the coordinate plane below:

5) F (-1,5)

6) N (-3, -3)

7) U (-2, 0)



Now, have the students go back to first graph and label the Quads (+, +) etc, label quads, label axes, and order